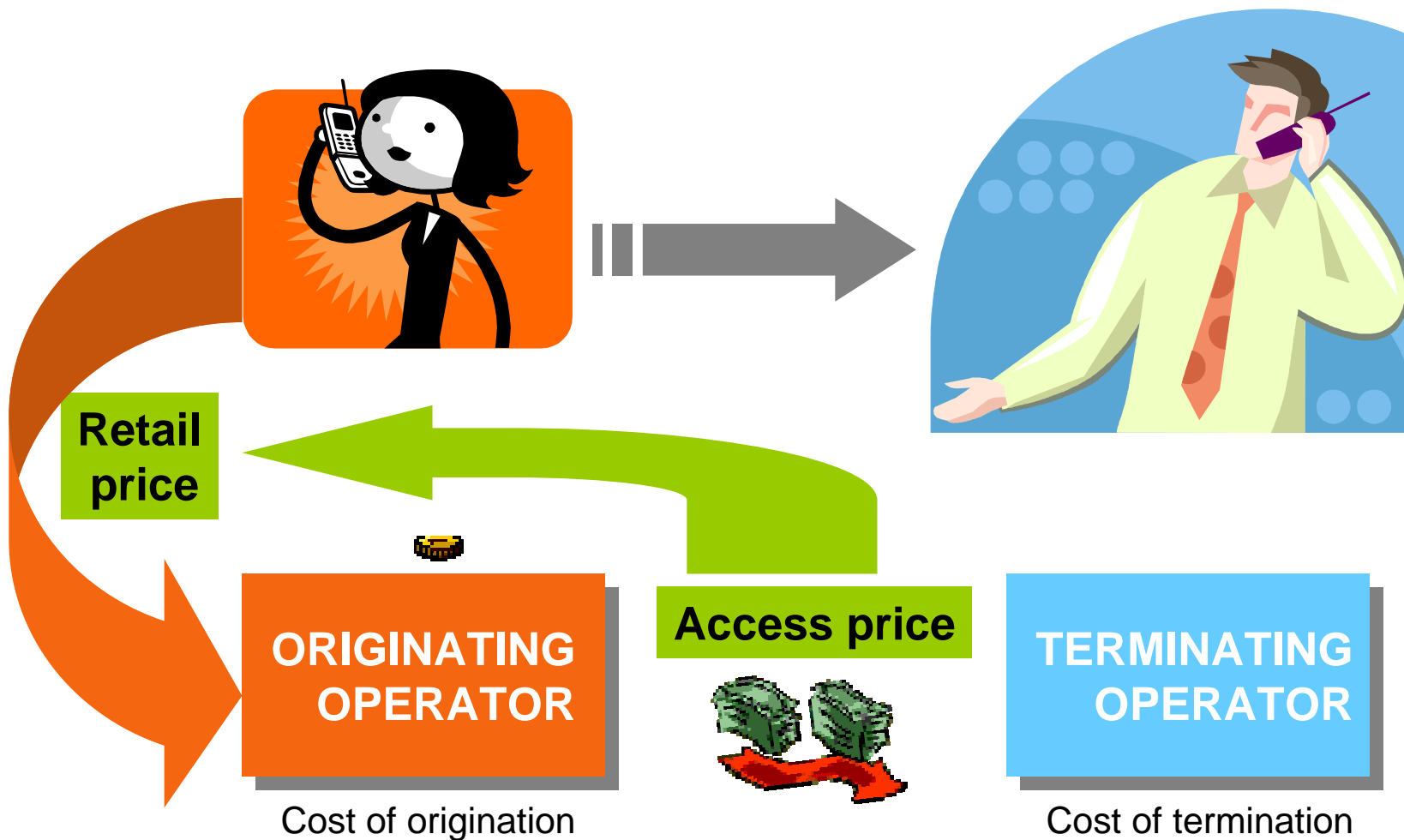


# **A Retail Benchmarking Approach to Efficient Two-way Access Pricing: Termination-Based Price Discrimination with Elastic Subscription Demand**

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# Network competition: access pricing



# Market for termination is monopoly

## Scope for ex-ante regulation:

- Bilateral negotiation of reciprocal access charges (collusion?)
- Regulate (= fix) access charges  
(Bill and Keep, Cost Based, Cost + return)
- Regulate access charge by fixing a benchmarking rule (Jeon-Hurkens, 2008)

# Results from fixed two-way access (without termination-based PD; with inelastic subscription demand)

- Linear pricing:
  - Collusion possibility
  - Optimal (Ramsey) access fee below cost
- Two-part tariffs:
  - Profit neutrality
  - Total welfare maximizing fee equal to cost

# Results from retail benchmarking

(without termination-based PD;  
with inelastic subscription demand)

- Linear pricing: there is one linear benchmarking rule that achieves the Ramsey prices.
- Two-part tariffs: there is a class of benchmarking rules (indexed by  $k$ ) resulting in marginal cost pricing, with higher  $k$  leading to lower fixed fees.
- Regulator needs no information on demands.

# Results from retail benchmarking

(without termination-based PD;  
with inelastic subscription demand)

**Intuition:** When the access charge to be paid by a network depends positively on its own (average) retail price, the network has incentive to lower retail price. Such a retail benchmarking approach thus intensifies competition in the retail market.

# This paper: Extensions

- Termination-based price discrimination
  - Fixed fee, on-net and off-net var. prices
- Elastic subscription demand
  - Consumers may remain unsubscribed
  - Lower fixed fees will increase subscription
  - Logit model (with outside option)

# Outline

1. Logit Model with Outside Option:
  - Rational expectations
2. Fixed Access Charges
  - Equilibrium
  - Business stealing vs. Network externalities
  - Comparative statics
3. Retail Benchmarking Rule
  - Equilibrium, Profits, Welfare, Subscription
4. Conclusion

# Model: Supply

## Costs:

$f$  fixed cost of serving a customer

$c_T$  the marginal cost of terminating a call

$c$  the marginal cost of a call

Duopolists set  $(F_i, p_i, \hat{p}_i)$

# Model: Demand for Calls

- $u(q)$ : concave increasing utility from calls of length  $q$
- $q(p)$ : demand function with  $u'(q(p))=p$
- $v(p)=u(q(p)) - pq(p)$

# Model: Demand for subscription

Consumers form expectations about number of subscribers

$$\beta_0, \beta_1, \beta_2 \geq 0 \text{ with } \beta_0 + \beta_1 + \beta_2 = 1.$$

Random utility from subscribing to network:

$$U_1 = V_1 + \mu\varepsilon_1 = \beta_1 v(p_1) + \beta_2 v(\hat{p}_1) - F_1 + \mu\varepsilon_1$$

$$U_2 = V_2 + \mu\varepsilon_2 = \beta_2 v(p_2) + \beta_1 v(\hat{p}_2) - F_2 + \mu\varepsilon_2$$

$$U_0 = V_0 + \mu\varepsilon_0$$

Subscribers:

$$\alpha_i = \frac{\exp[V_i / \mu]}{\sum_{k=0}^2 \exp[V_k / \mu]}$$

# Model: Rational Expectations

Expectations are rational iff  $\alpha_i = \beta_i$  .

Rational expectations exist for any pricing schedules.

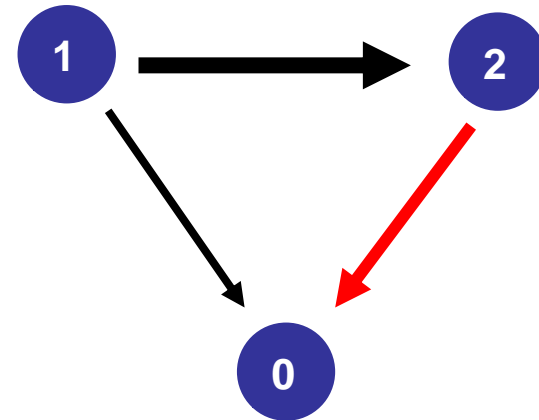
Rational expectations are unique if  $\mu > v(c)/4$  .

# Model: Rational Expectations

An increase in  $F_1$  causes  
a decrease in  $\alpha_1$

a decrease in  $\alpha_1 + \alpha_2$

an ambiguous effect in  $\alpha_2$



$$\frac{\partial \alpha_2}{\partial F_1} > 0 \Leftrightarrow \Delta = \mu - \alpha_0 v(\hat{p}_2) > 0$$

**Net Business Stealing**

$$\frac{\partial \alpha_2}{\partial F_1} < 0 \Leftrightarrow \Delta = \mu - \alpha_0 v(\hat{p}_2) < 0$$

**Net Network Externality**

# Fixed Access Charge $h$

$$R(p) = (p - c)q(p)$$

$$\Pi_i = \alpha_i \left[ \underbrace{\alpha_i R(p_i) + \alpha_j R(\hat{p}_i) + F_i - f}_{\text{Retail profit per customer}} \right]$$

Retail profit per customer

$$+ \underbrace{\alpha_i \alpha_j (a - c_T)(q(\hat{p}_j) - q(\hat{p}_i))}_{\text{Net Access Revenue}}$$

Net Access Revenue

Maximizing profit requires perceived marginal cost pricing:  $p_i = c, \hat{p}_i = c + a - c_T$

# Fixed Access Charge $h$

Given perceived marginal cost pricing

$$\hat{c} = c + a - c_T$$

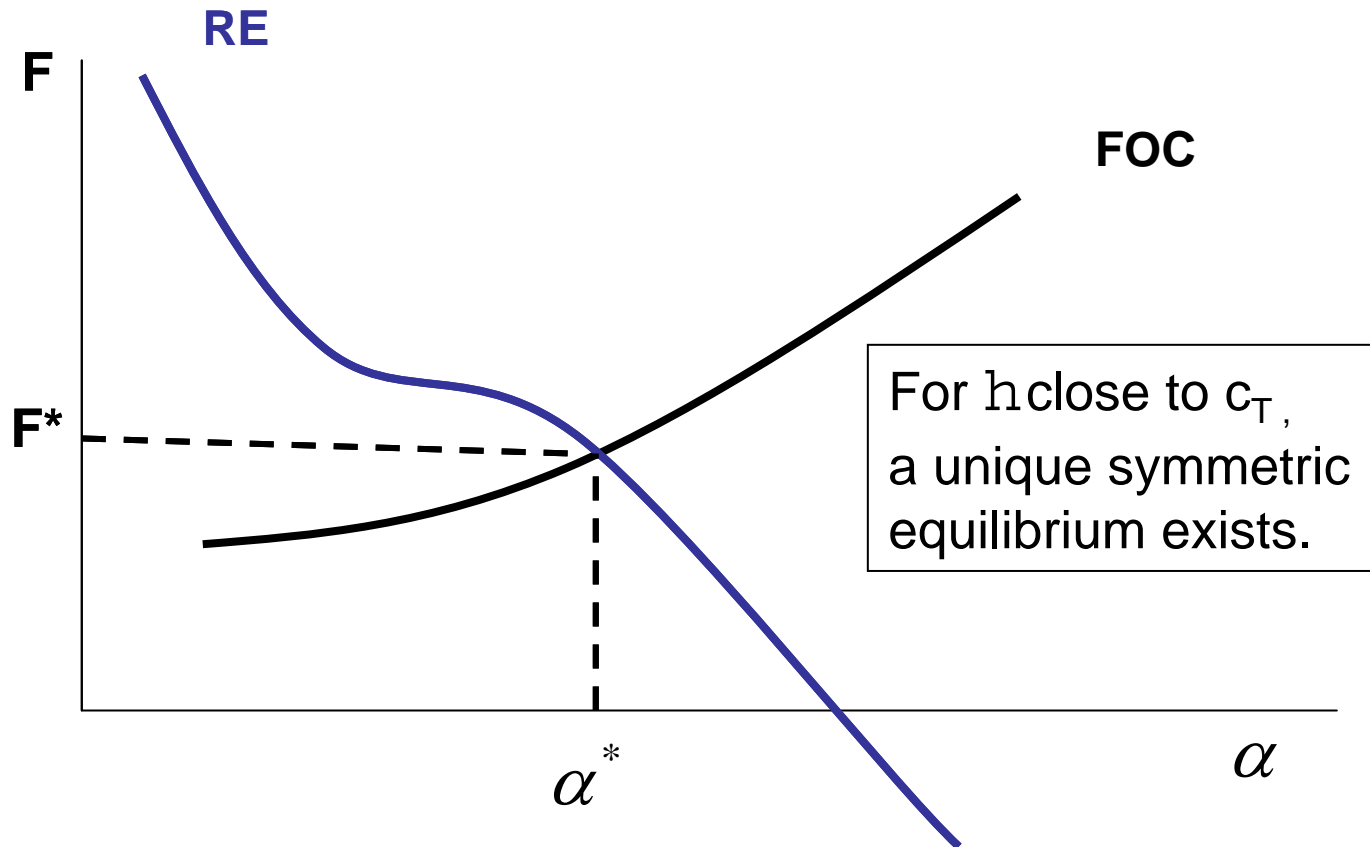
$$\Pi_i = \alpha_i \left[ \alpha_j R(\hat{c}) + F_i - f \right]$$

Symmetric equilibrium fixed fees and subscription are given by FOC and RE

$$F = F^{equil}(\alpha, a)$$

$$F = F^{RE}(\alpha, a) := \alpha(v + \hat{v}) - V_0 - \mu \ln \left[ \frac{\alpha}{1 - 2\alpha} \right]$$

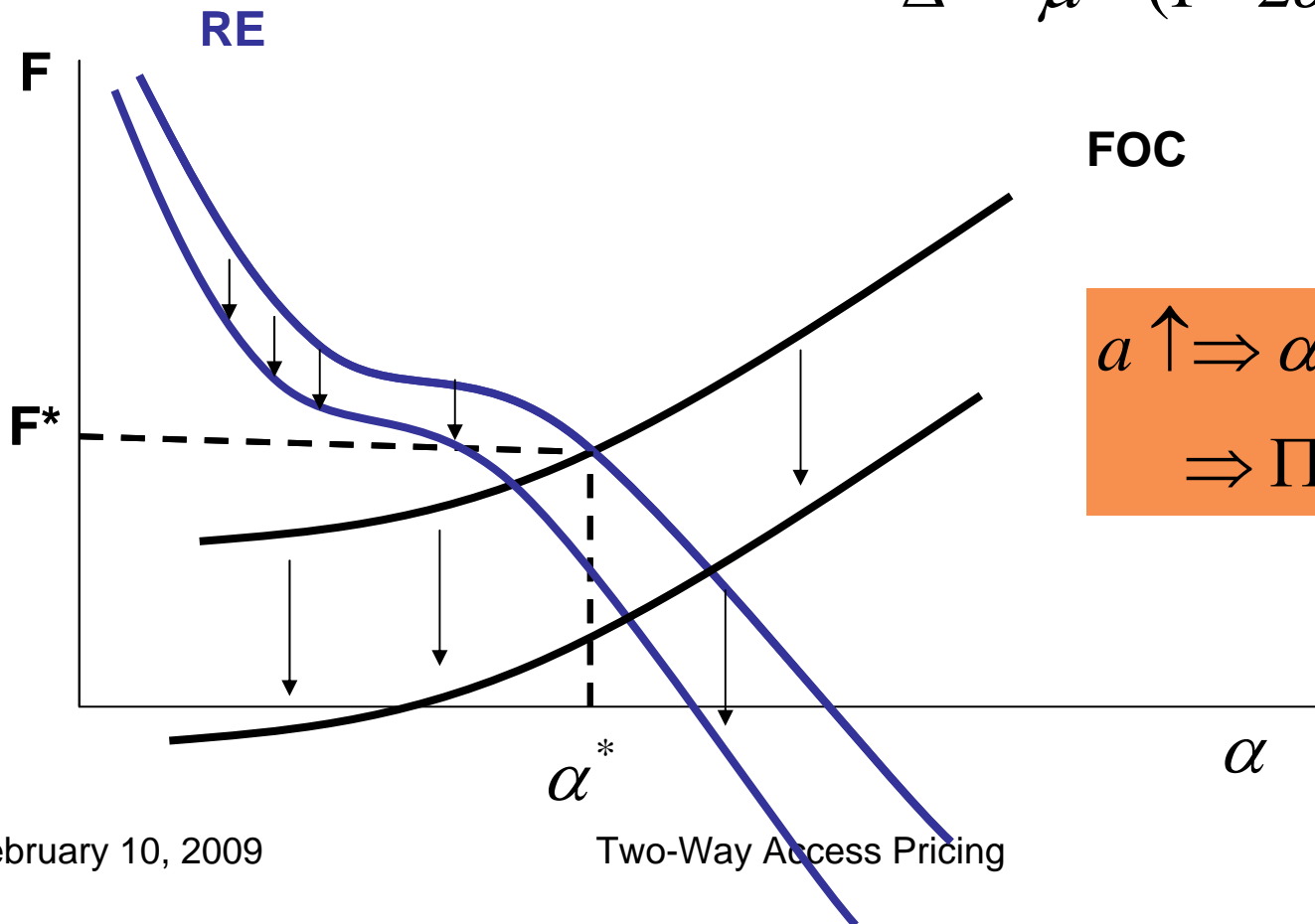
# Fixed Access Charge $h$



# Comparative statics at $h=c_T$

## Net Business Stealing Effect

$$\Delta^* = \mu - (1 - 2\alpha^*)v(c) > 0$$



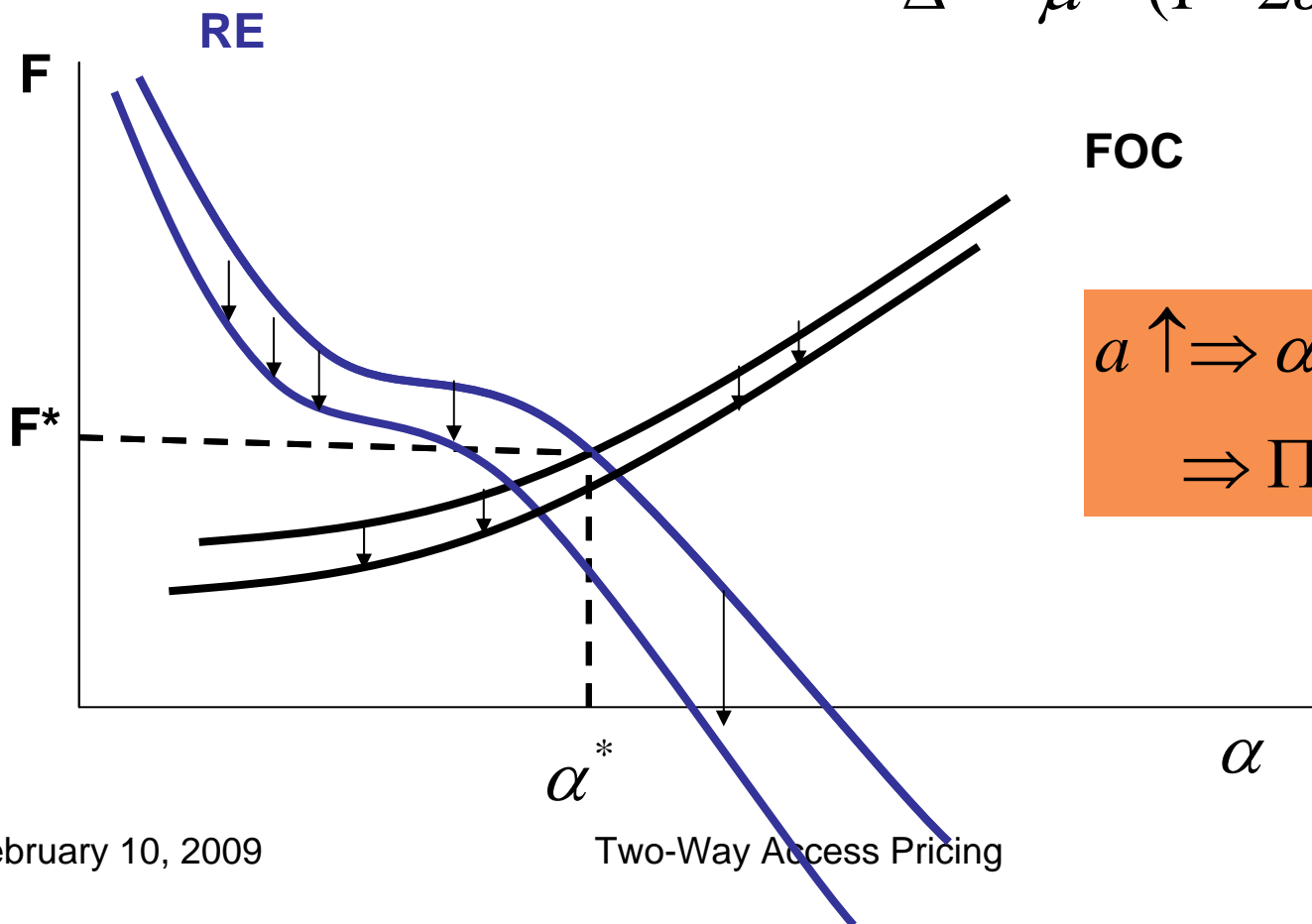
$$a \uparrow \Rightarrow \alpha^* \uparrow$$

$$\Rightarrow \Pi \downarrow, CS \uparrow, TS \uparrow$$

# Comparative statics at $h=c_T$

## Net Network Externality

$$\Delta^* = \mu - (1 - 2\alpha^*)v(c) < 0$$



$a \uparrow \Rightarrow \alpha^* \downarrow$   
 $\Rightarrow \Pi \downarrow, CS \downarrow, TS \downarrow$

# Comparative statics at $h=c_T$

- Firms always prefer  $h < c_T$ 
  - Either to soften competition  
(Gans&King,2000; Calzada&Valletti,2008)
  - Or to internalize network externality  
(Dessein,2003)
- Regulator prefers  $h < c_T$  only when the network externality effect dominates.

# Retail Benchmarking Approach

Retail profit /customer gross of fixed cost

$$\pi_i(a) = \alpha_i R(p_i) + \alpha_j (\hat{p}_i - (c + a - c_T)) q(\hat{p}_i) + F_i$$

Total profit:

$$\Pi_i = \alpha_i [\pi_i(a) + \alpha_j (a - c_T) q(\hat{p}_j) - f]$$

Define access charge to be paid by i:

$$\lambda(a, k) = a + k \frac{\pi_i(a)}{q(\hat{p}_i)}$$

# Retail Benchmarking Approach

Total profit can be rewritten as:

$$\Pi_i = \alpha_i [(1 - k\alpha_j)\pi_i(a) - f] + k\alpha_i\alpha_j [\pi_j(a) + (a - c_T)q(\hat{p}_j)]$$

Max.  $\Pi_i$  is equivalent to  $\max \pi_i(a)$  if  $k \leq 1$ .

Hence, perceived marginal cost pricing:

$$p_i = c, \hat{p}_i = \hat{c},$$

# Retail Benchmarking Approach

Now

$$\Pi_i = \alpha_i [F_i + \alpha_j R(\hat{c}) - f] - k \alpha_i \alpha_j [F_i - F_j]$$

Competition in fixed fee, fiercer for larger k !

# Retail Benchmarking Approach

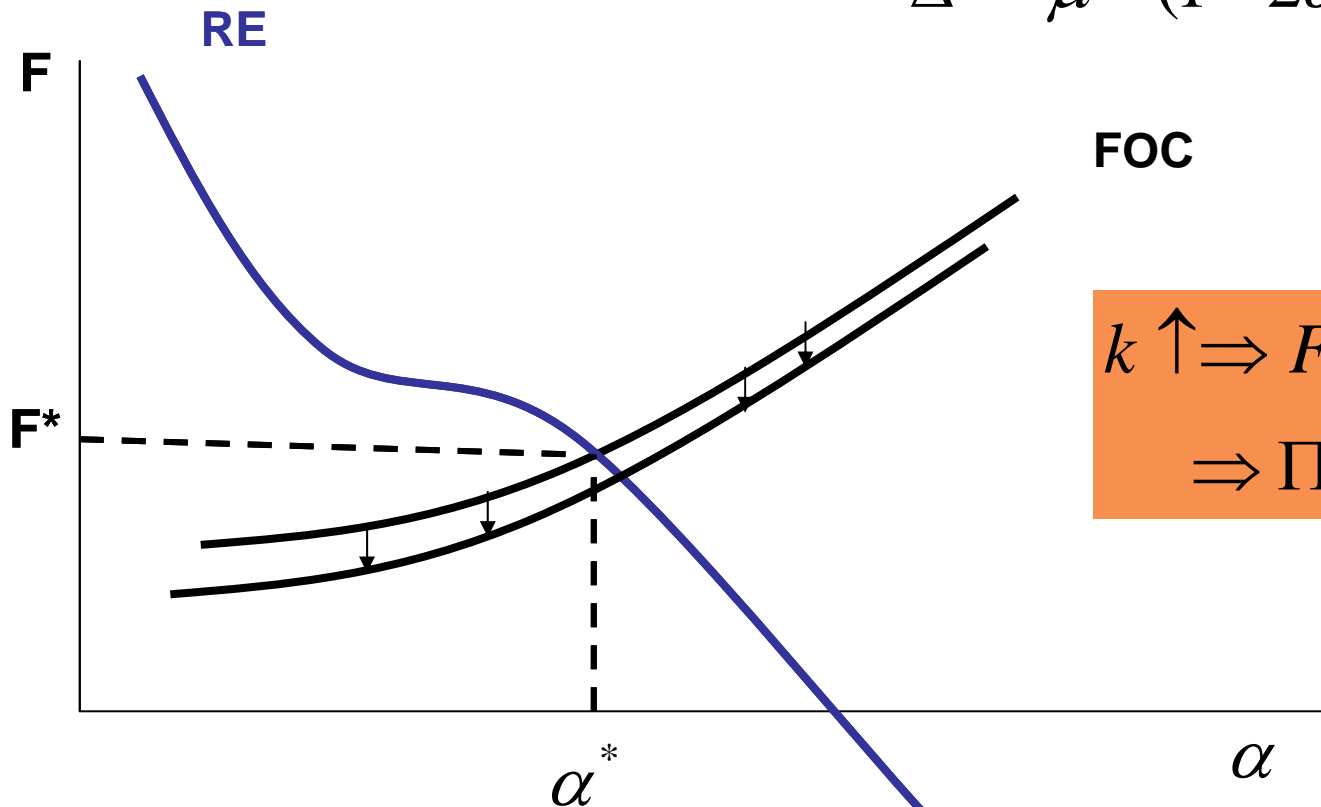
Consider  $\lambda(a, k)$  with  $a \approx c_T$  and  $k \leq 1$

1. Marginal cost pricing
2. Fixed fee decreases in  $k$ .
3. Can increase subscription without (further) distorting usage prices

# Comparative statics

## Net Network Externality

$$\Delta^* = \mu - (1 - 2\alpha^*)v(c) < 0$$



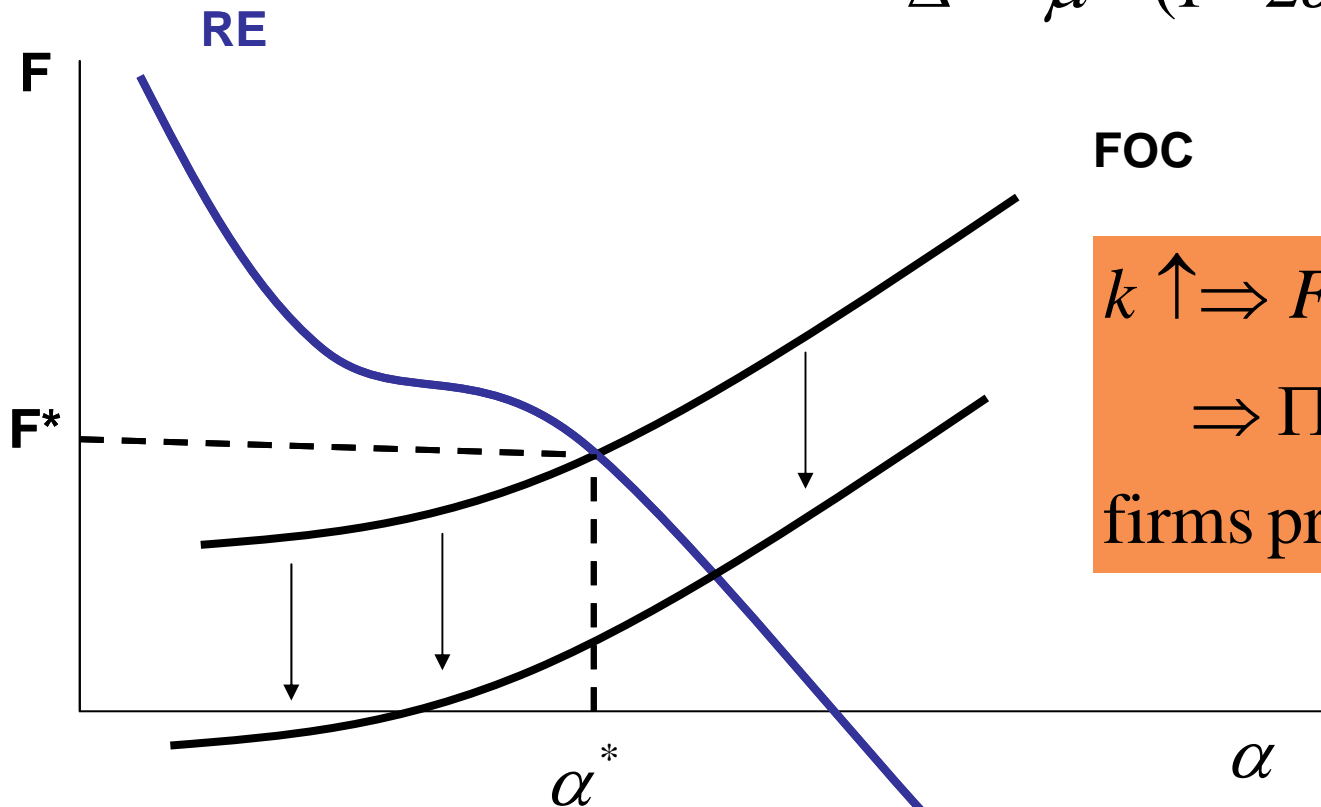
$$k \uparrow \Rightarrow F \downarrow, \alpha^* \uparrow$$

$$\Rightarrow \Pi \uparrow, CS \uparrow, TS \uparrow$$

# Comparative statics

## Net Business Stealing Effect

$$\Delta^* = \mu - (1 - 2\alpha^*)v(c) > 0$$



$k \uparrow \Rightarrow F \downarrow, \alpha^* \uparrow$   
 $\Rightarrow \Pi \downarrow, CS \uparrow, TS \uparrow$   
 firms prefer  $k < 0$

# Conclusion

Retail benchmarking approach works:

- $k > 0$  increases competition in fixed fees
- And thus increases subscription
- Without distorting usage prices
- Any fixed termination charge is Pareto dominated by some retail benchmarking rule (possibly  $k < 0$ )